

# Chiral Four-Nucleon Force in Ab Initio Nuclear Structure

Stefan Schulz and Robert Roth

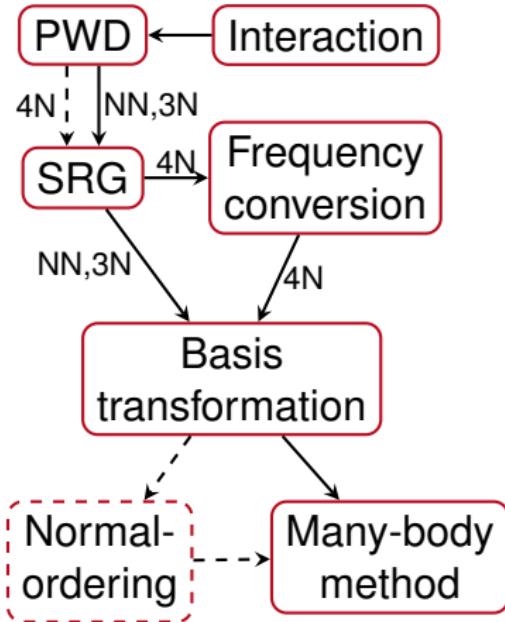
*Technische Universität Darmstadt*



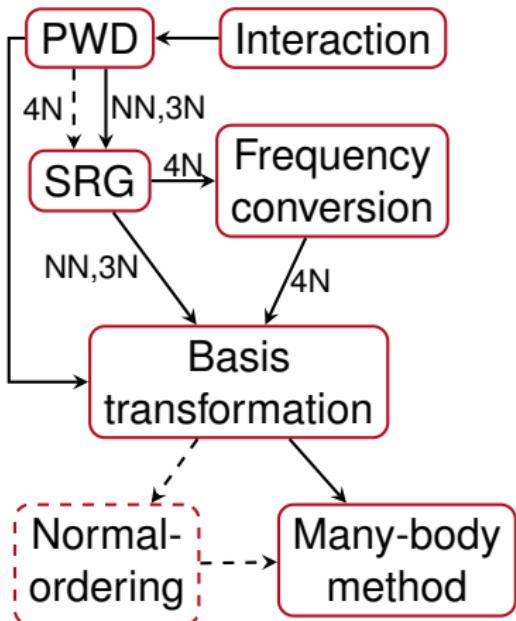
# Why Four-Body Forces?

- ▶ Effect of SRG-induced 4N contributions increases with number of nucleons
  - ▶ Fine-tune interaction
  - ▶ Change SRG generator
- ▶ Effect of initial 4N contributions?
  - ▶ Similar scaling with number of nucleons?
- ▶ Goal: Consistent order-by-order calculations for chiral Interactions
  - ▶ Chiral 4N interaction necessary starting from  $N^3LO$ !

# Framework

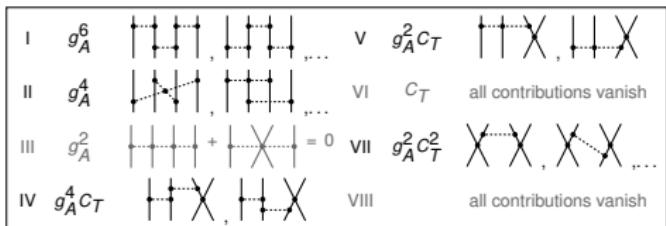


# Framework



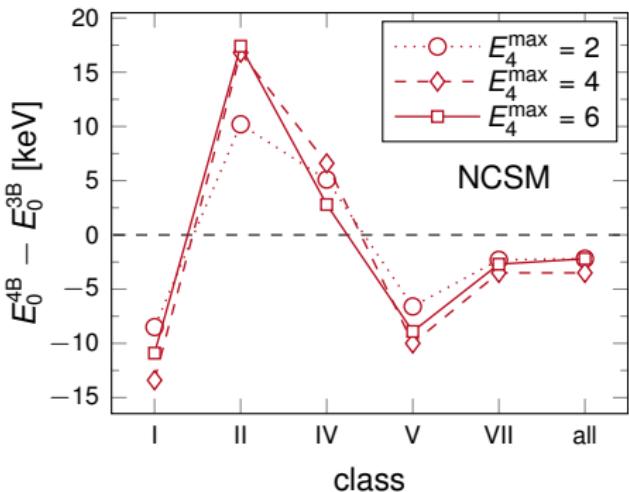
## Chiral 4N at $N^3\text{LO}$

- ▶ PWD for 5 classes
  - ▶ 11 different operator structures
  - ▶ Crosschecks: Monte-Carlo integration
- ▶ Limit on partial wave &  $E_4^{\max}$
- ▶ Local regulator  $\Rightarrow$  speedup
$$\exp \left[ - \left( \frac{(\vec{n}'_1 - \vec{n}_1)^2 + (\vec{n}'_2 - \vec{n}_2)^2 + (\vec{n}'_3 - \vec{n}_3)^2}{3\Lambda^2} \right)^2 \right]$$



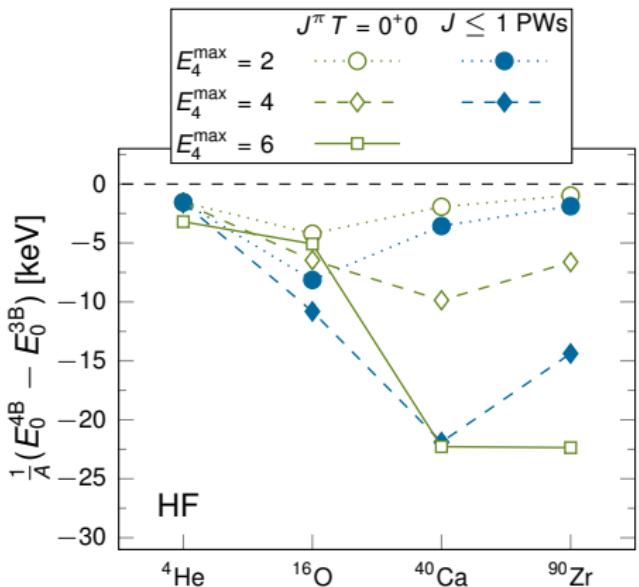
# Ground State of $^4\text{He}$

- ▶ Cancellation between different classes
- ▶ Not completely converged
- ▶ Differs from previous estimate
  - A. Nogga et al., EPJ Web of Conferences 3, 05006 (2010).
  - ▶ Sensitive to NN+3N interaction
  - ▶ Different regulator, model space, ...
- ▶ Weak overall effect



$N_{\max} = 20, \hbar\omega = 24 \text{ MeV}, \alpha_{2B} = \alpha_{3B} = 0.08 \text{ fm}^4$   
 NN interaction at  $\text{N}^3\text{LO}$  with  $\Lambda = 500 \text{ MeV/c}$  D. R. Entem et al., PRC 68, 041001 (2003)  
 3N interaction at  $\text{N}^2\text{LO}$  with  $\Lambda = 400 \text{ MeV/c}$  R. Roth et al., PRL 109, 052501 (2012)  
 4N interaction with  $\Lambda_{4B} = 400 \text{ MeV/c}$  and  $C_T = 0.21 \text{ fm}^2$  E. Epelbaum, The EPJ A 34, 2, 197 (2007).

# Heavier Nuclei



- ▶ Contribution increases with number of nucleons
- ▶ Not converged w.r.t.  $E_4^{\max}$  or  $J$
- ▶ Weak overall effect

$e_{\max} = 8, \hbar\omega = 24 \text{ MeV}, \alpha_{2B} = \alpha_{3B} = 0.08 \text{ fm}^4$

NN interaction at  $N^3\text{LO}$  with  $\Lambda = 500 \text{ MeV}/c$  D. R. Entem et al., PRC 68, 041001 (2003)

3N interaction at  $N^2\text{LO}$  with  $\Lambda = 400 \text{ MeV}/c$  R. Roth et al., PRL 109, 052501 (2012)

4N interaction with  $\Lambda_{4B} = 400 \text{ MeV}/c$  and  $C_T = 0.21 \text{ fm}^2$  E. Epelbaum, The EPJ A 34, 2, 197 (2007).