

# From Few Nucleons to X-ray Burst Abundances: Reaction Rates from Overlaps of SA-NCSM and Cluster Bases

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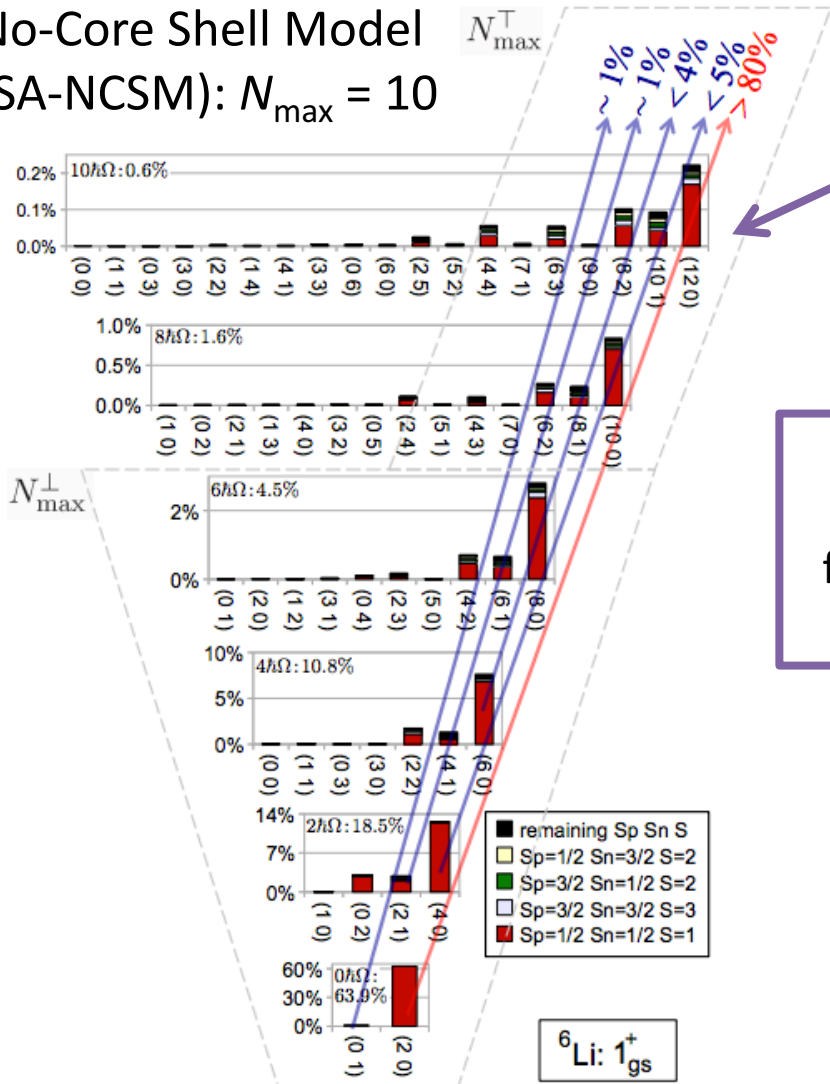
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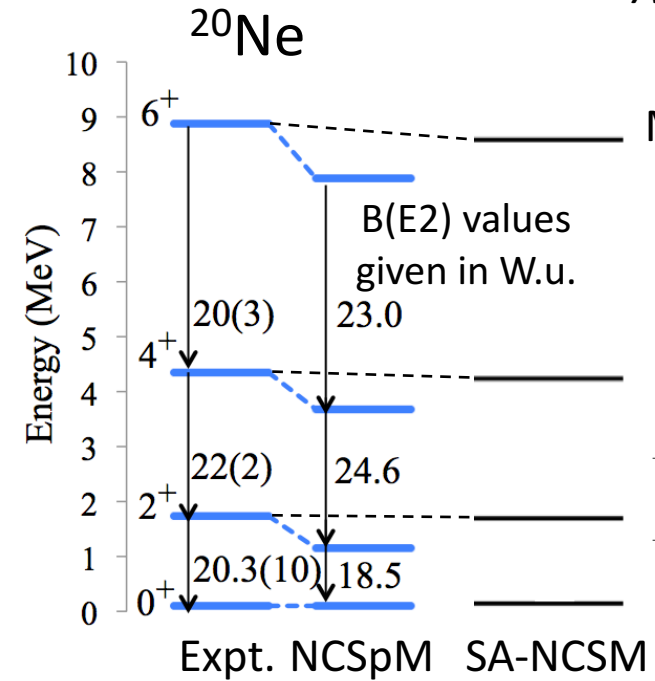
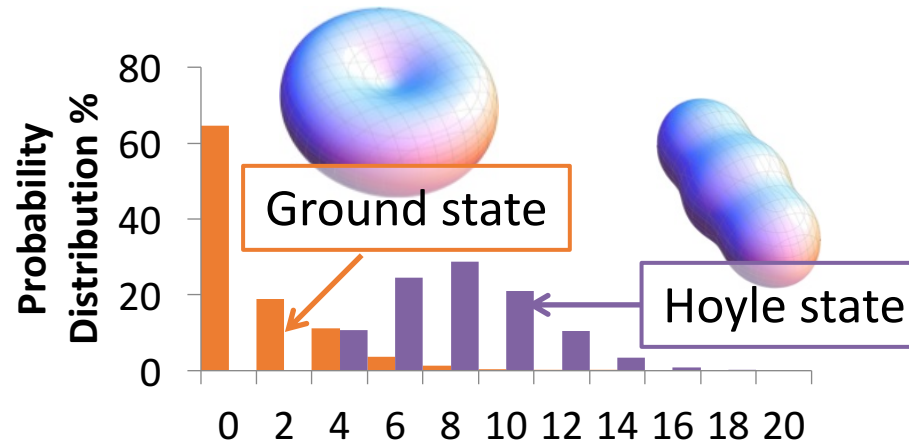
# ROLE OF SYMMETRY-ADAPTED (SA) BASIS AND SYMPLECTIC SYMMETRY

*Ab initio* Symmetry-Adapted  
No-Core Shell Model  
(SA-NCSM):  $N_{\max} = 10$

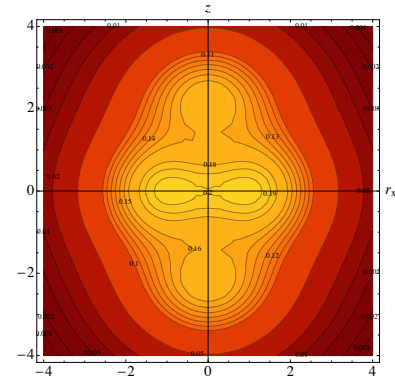


Symplectic symmetry  
emerges from *ab initio*  
studies

Symplectic symmetry  
exposes cluster  
formation – e.g., in the  
Hoyle state of  $^{12}\text{C}$



*Ab initio* description  
of  $^{20}\text{Ne}$   
(N2L0opt,  $\hbar\Omega=15$   
MeV, 13 HO shells)



Schematic NCSpM  
reproduces observables:  
spectrum, rms radii,  
quadrupole moments

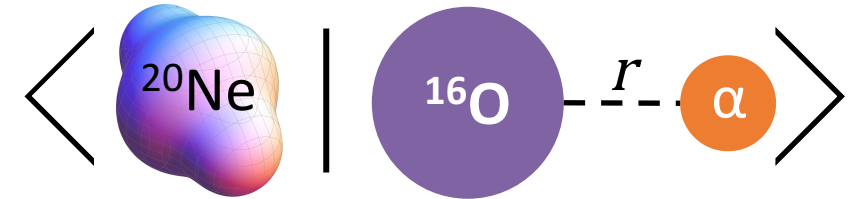
# PROBING CLUSTER STRUCTURE

$$u_l(r) = \langle \psi_A | \mathcal{A} \{ \phi_{A-f} \times \phi_f \} Y_{l0} \frac{\delta(r-a)}{ra} \rangle$$

A-particle wave function eigenstates  
in symplectic basis:

$$|\psi_A\rangle = \sum_Q c_Q |Q[\gamma(\lambda\mu)]\rangle$$

Expand  $\delta$ -function in  
orthonormal harmonic  
oscillator basis



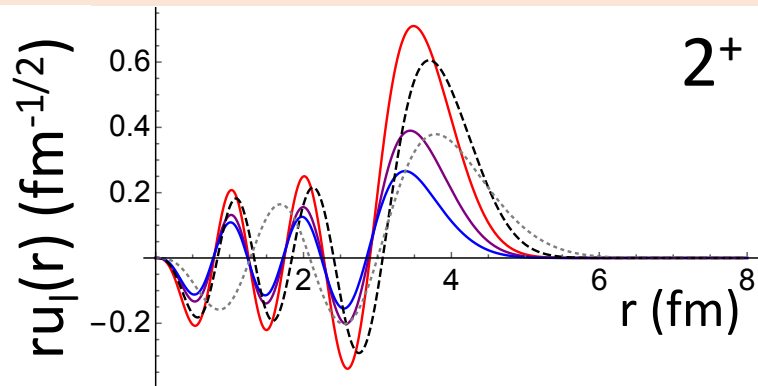
$$u_l(r) = \sum_Q R_{Q,l}(r) c_Q \langle Q[\gamma(\lambda\mu)] | \{ \{ (\lambda_{A-f} \mu_{A-f}) \times (\lambda_f \mu_f) \}^{(\lambda_c \mu_c)} \times (Q0) \}_l^{(\lambda\mu)} \rangle$$

Overlaps computed recursively:

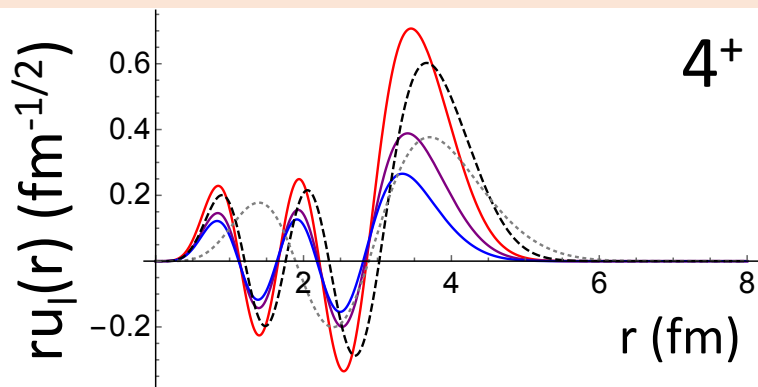
$$\begin{aligned} & \langle [N\gamma'(\lambda'\mu') \times (20)](\lambda\mu)\xi | [(\lambda_c\mu_c) \times (Q+2,0)](\lambda\mu)\xi \rangle \\ &= \sqrt{\dim(Q0)} U [(\lambda_c\mu_c)(Q0)(\lambda\mu)(20); (\lambda'\mu'); (Q+20)] \langle N\gamma'(\lambda'\mu')\xi' | [(\lambda_c\mu_c) \times (Q0)](\lambda'\mu')\xi' \rangle \end{aligned}$$

# EVIDENCE FOR CLUSTERING

$^{24}\text{Mg}$

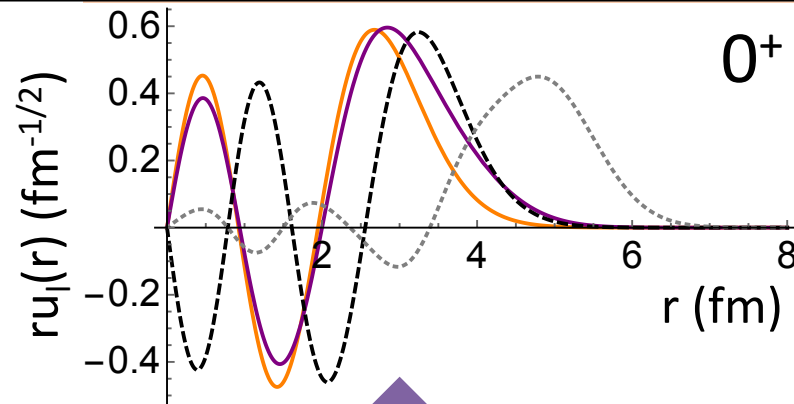


$\{^{20}\text{Ne} + \alpha\}_{\text{NCSpM}}: (8\ 0)$   
 $\{^{16}\text{O} + ^8\text{Be}\}_{\text{NCSpM}}: (4\ 0)$   
 $\{^{12}\text{C} + ^{12}\text{C}\}_{\text{NCSpM}}: (0\ 8), (2\ 4), (4\ 0)$



$^{16}\text{O}: \{^{12}\text{C} + \alpha\}$

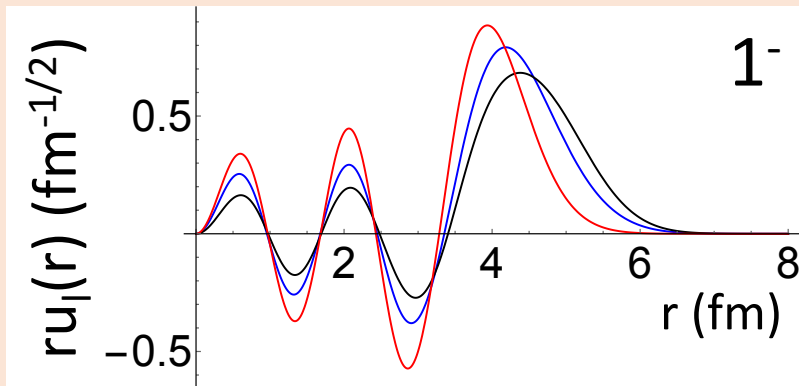
NCSpM ( $N_{\text{max}}=16$ ): (0 0), (4 2), (8 4)  
 SA-NCSM ( $N_{\text{max}}=10$ ): (0 0)



Evidence of cluster formation developing for the Hoyle-like second  $0^+$  state in  $^{16}\text{O}$  described by the (8 4) irrep in the NCSpM

We can consider multiple different partitions of clusters

$^{20}\text{Ne}: \{^{16}\text{O} + \alpha\}$



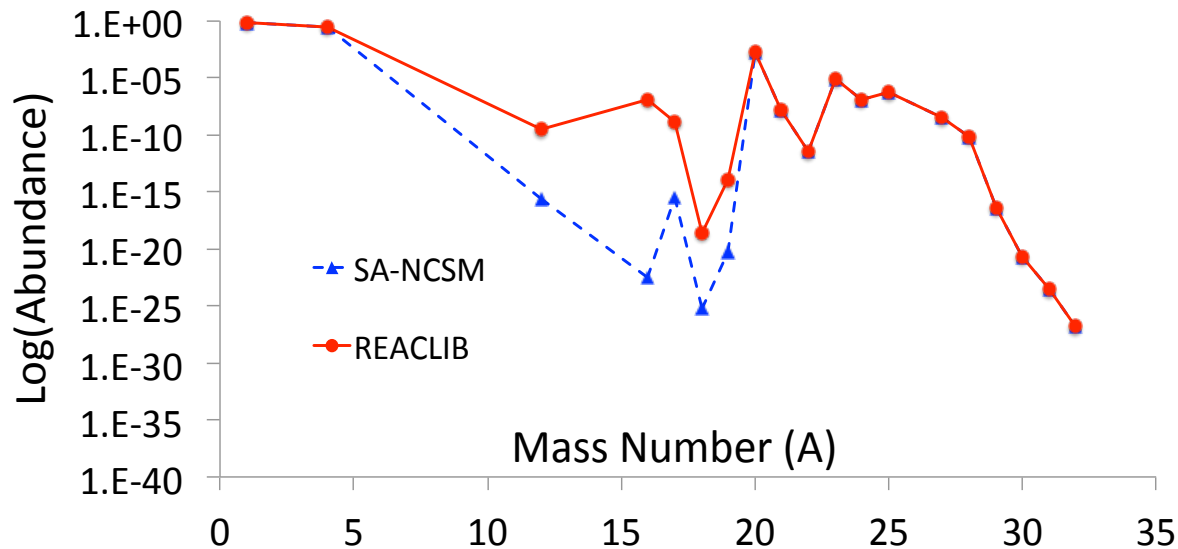
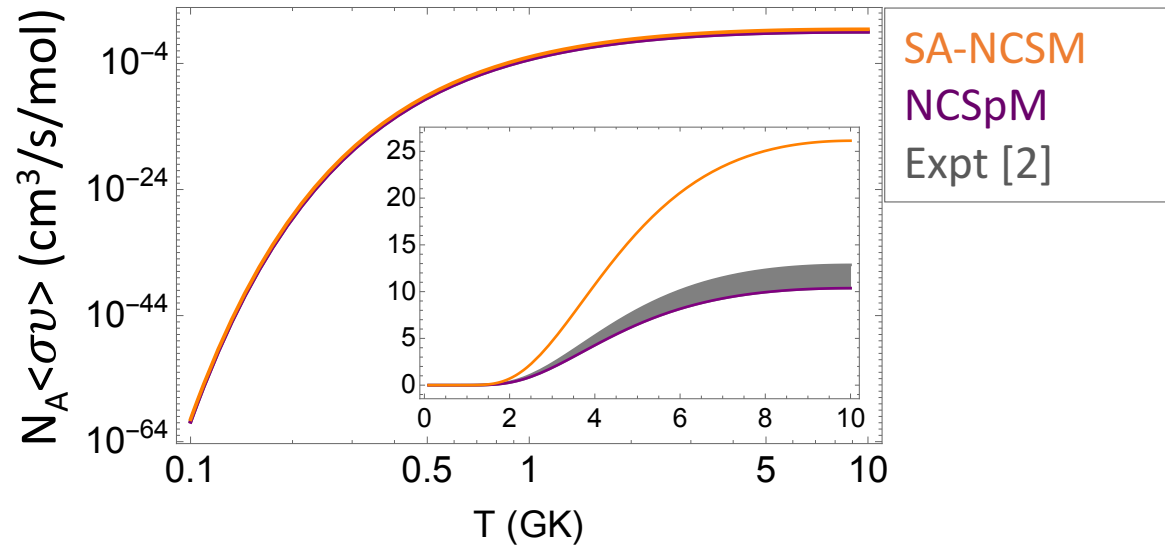
SA-NCSM  $N_{\text{max}}=3$  SA-NCSM  $N_{\text{max}}=11$   
 NCSpM  $N_{\text{max}}=13$

## Decay Widths ( $\Gamma_\alpha$ )

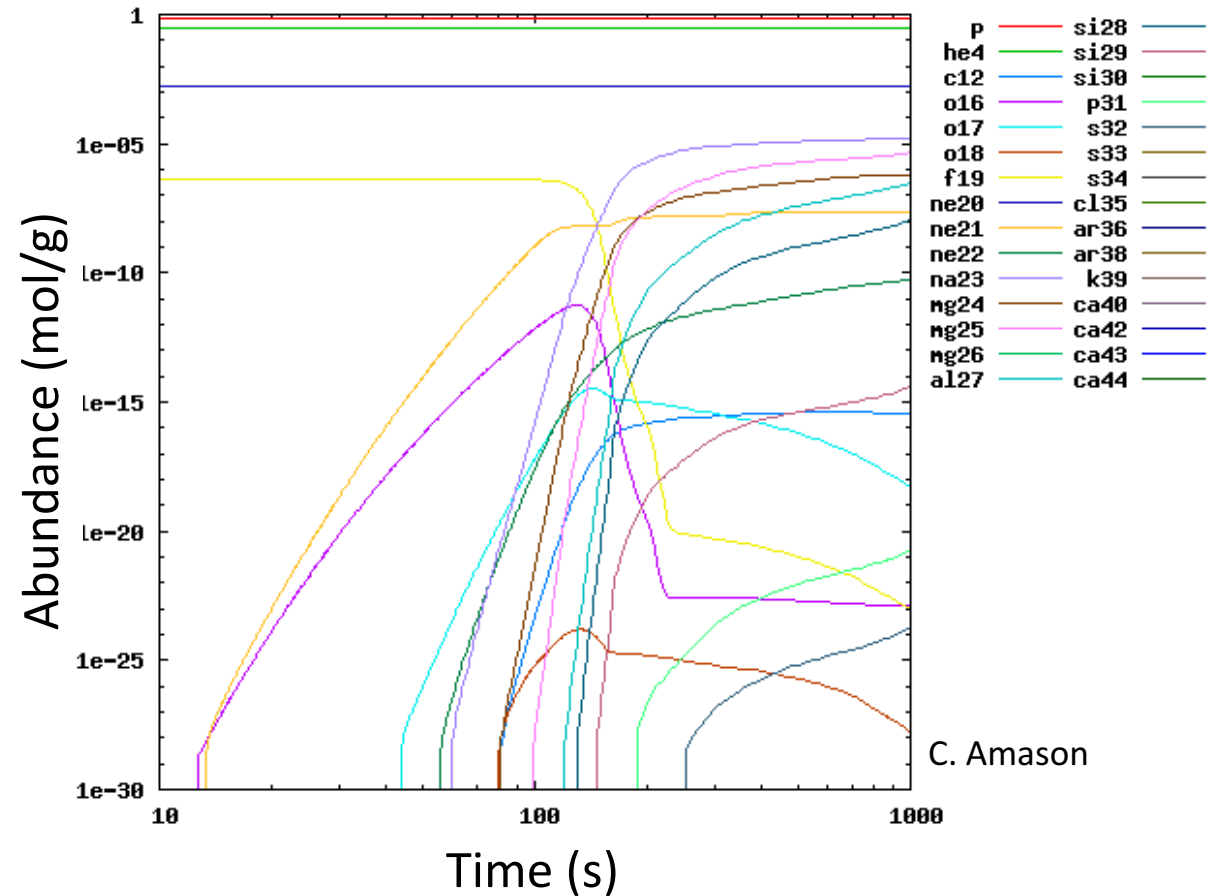
NCSpM ( $N_{\text{max}}=13$ )	25
SA-NCSM ( $N_{\text{max}}=3$ )	5.7
SA-NCSM ( $N_{\text{max}}=11$ )	63
Experimental [2]	28(3)

# X-RAY BURST NUCLEOSYNTHESIS

Reaction Rate  $^{16}\text{O}(\alpha,\gamma)^{20}\text{Ne}[1^-]$



XRB nucleosynthesis simulation

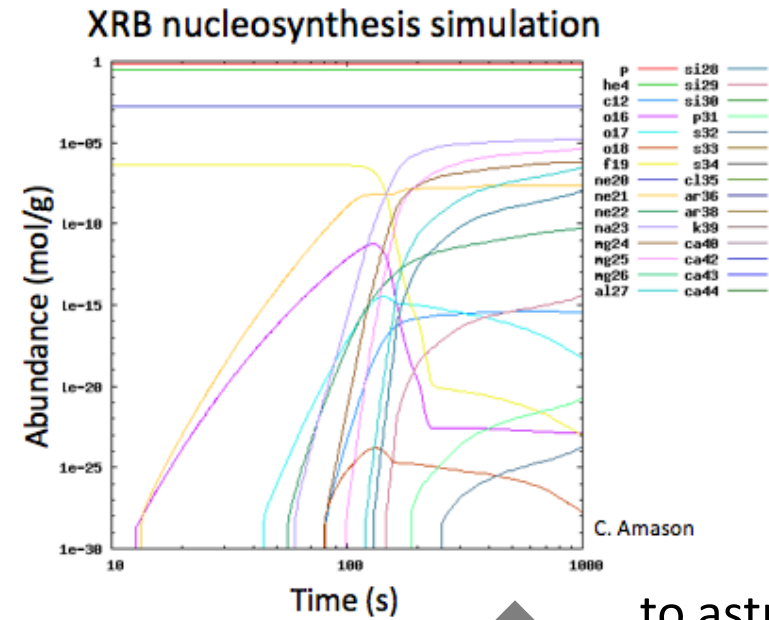


Using reaction rates computed with *ab initio* structure input, we can consider the development of nuclear abundances in astrophysical simulations and final abundance patterns.

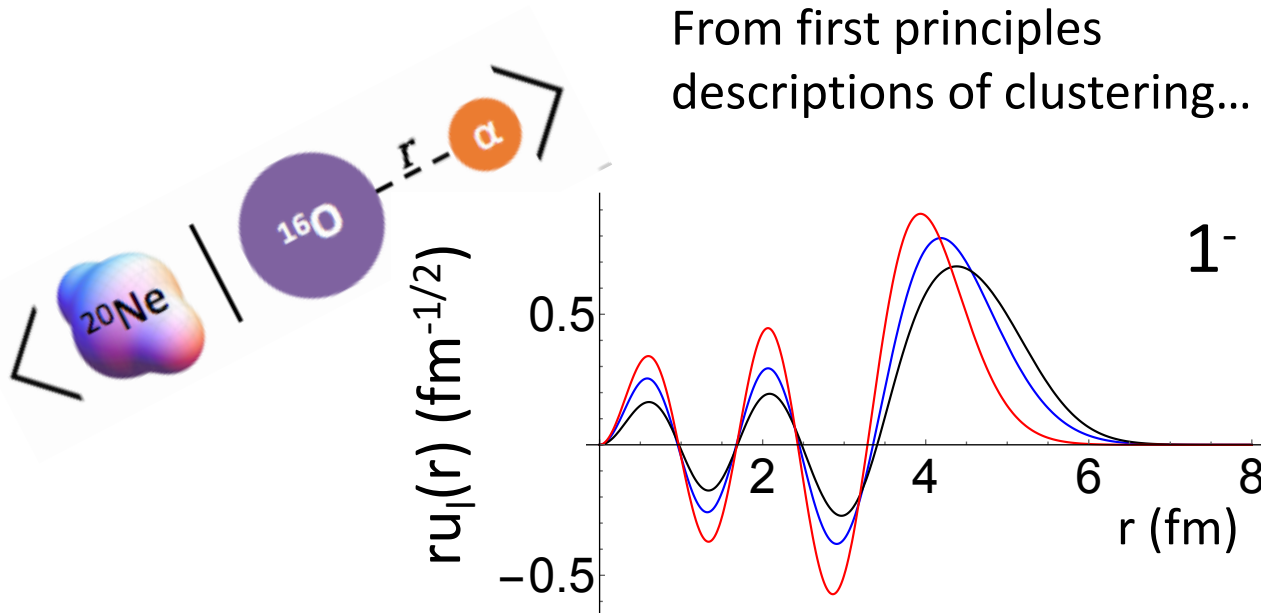
# THANK YOU

## REFERENCES

- [1] Y. Suzuki, *Nuc Phys A* **448**, 395 (1986)
- [2] H. Constantini *et al.*, *Phys Rev C* **82**, 035802 (2010)
- [3] A. C. Dreyfuss *et al.*, *Phys Lett B* **727** (2013)
- [4] K. D. Launey *et al.*, *Prog Part Nuc Phys* **89** (2016)
- [5] G. K. Tobin *et al.*, *Phys Rev C* **89** (2014)



From first principles descriptions of clustering...



...to astrophysical simulations!

