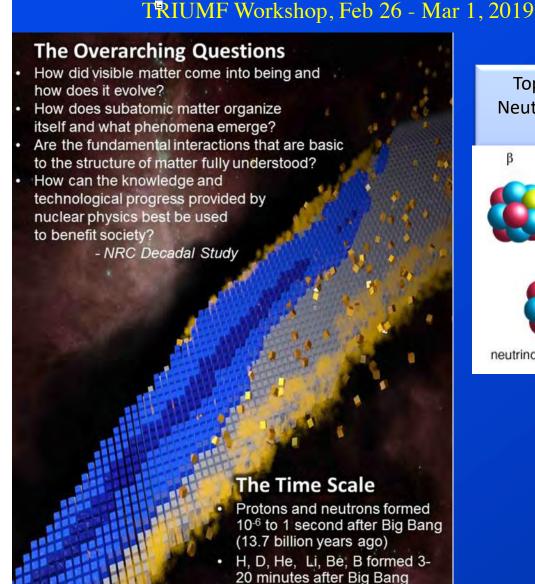
No Core Shell Model (NCSM) With Consistent Electroweak Interactions and Other Recent Developments James P. Vary, Iowa State University

Other elements born over the

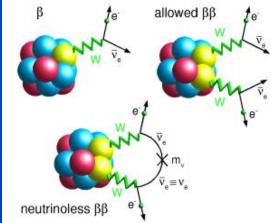
next 13.7 billion years







Topical Collaboration on Neutrinos and Fundamental Symmetries







No-Core Configuration Interaction calculations

Barrett, Navrátil, Vary, Ab initio no-core shell model, PPNP69, 131 (2013)

Given a Hamiltonian operator

$$\hat{\mathbf{H}} = \sum_{i < j} \frac{(\vec{p_i} - \vec{p_j})^2}{2 m A} + \sum_{i < j} V_{ij} + \sum_{i < j < k} V_{ijk} + \dots$$

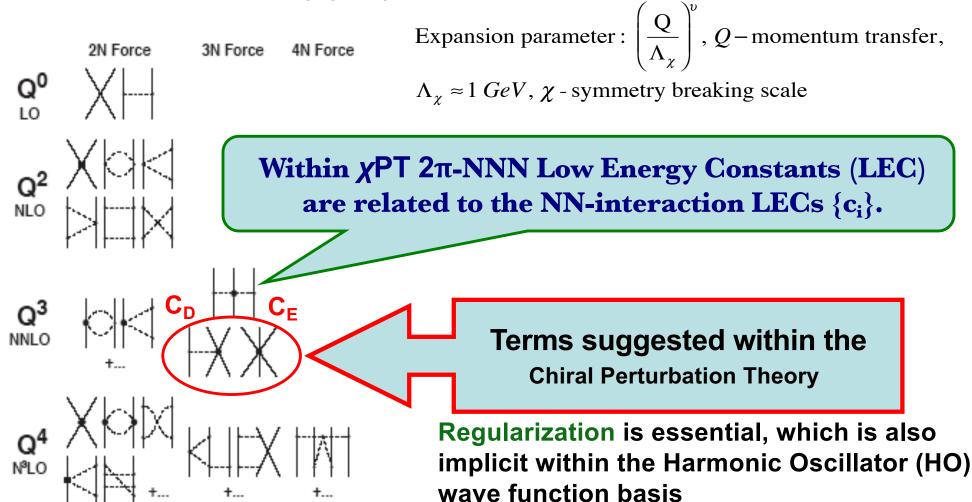
solve the eigenvalue problem for wavefunction of A nucleons

$$\mathbf{\hat{H}} \Psi(r_1, \dots, r_A) = \lambda \Psi(r_1, \dots, r_A)$$

- Expand eigenstates in basis states $|\Psi\rangle = \sum a_i |\Phi_i\rangle$
- ullet Diagonalize Hamiltonian matrix $H_{ij} = \langle \Phi_j | \hat{\mathbf{H}} | \Phi_i
 angle$
- No Core Full Configuration (NCFC) All A nucleons treated equally
- Complete basis exact result
- In practice
 - truncate basis
 - study behavior of observables as function of truncation

Effective Nucleon Interaction (Chiral Perturbation Theory)

Chiral perturbation theory (χ PT) allows for controlled power series expansion



R. Machleidt and D.R. Entem, Phys. Rep. 503, 1 (2011);

E. Epelbaum, H. Krebs, U.-G Meissner, Eur. Phys. J. A51, 53 (2015); Phys. Rev. Lett. 115, 122301 (2015)

Calculation of three-body forces at N³LO

Low
Energy
Nuclear
Physics
International
Collaboration



J. Golak, R. Skibinski, K. Tolponicki, H. Witala



E. Epelbaum, H. Krebs



A. Nogga



R. Furnstahl



S. Binder, A. Calci, K. Hebeler, J. Langhammer, R. Roth



P. Maris, J. Vary



H. Kamada



U.-G Meissner

Goal

Calculate matrix elements of 3NF in a partialwave decomposed form which is suitable for different few- and many-body frameworks

Challenge

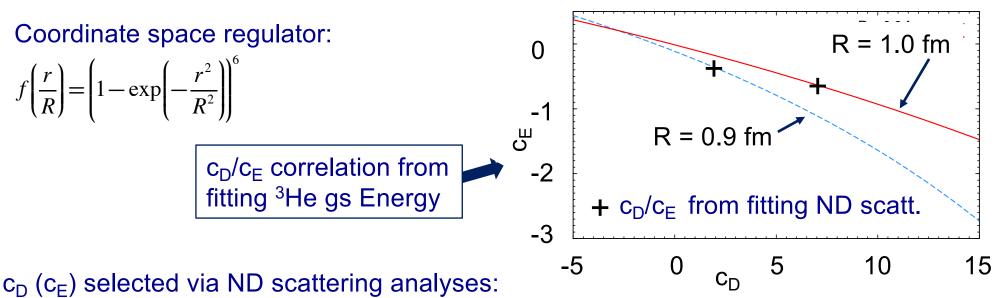
Due to the large number of matrix elements, the calculation is extremely expensive.

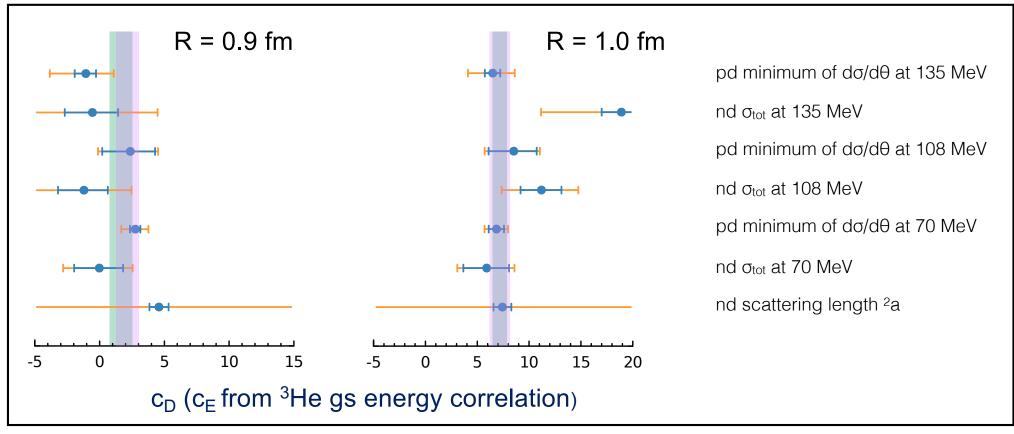
Strategy

Develop an efficient code which allows to treat arbitrary local 3N interactions.

(Krebs and Hebeler)

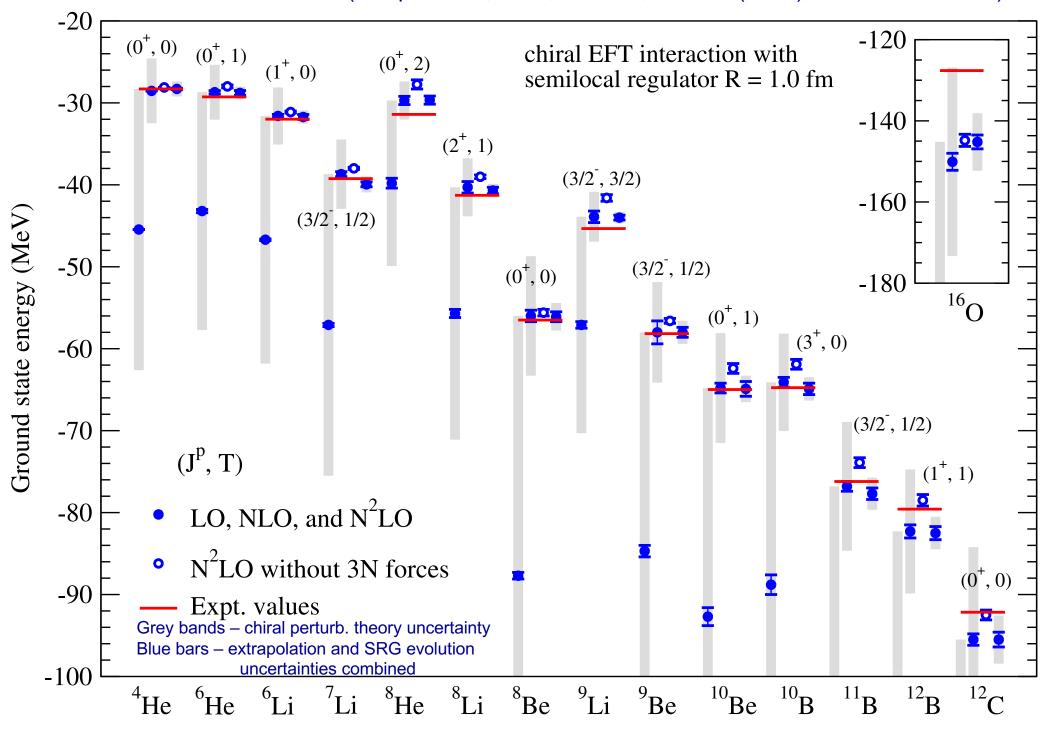
Additional Goal: Develop consistent chiral EFT theory for electroweak operators



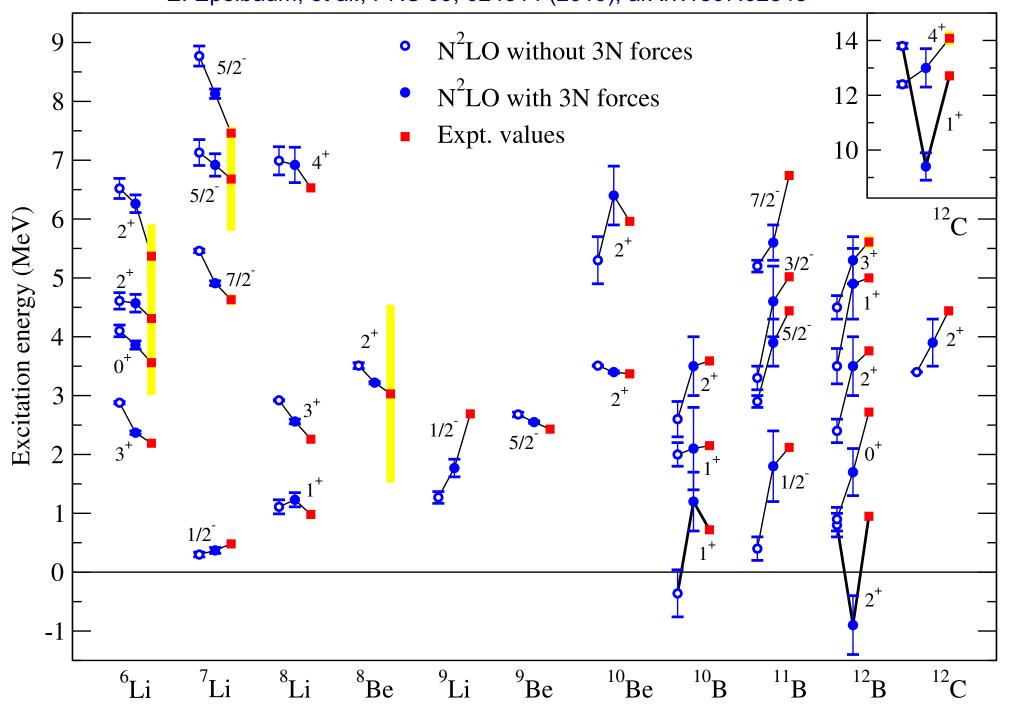


LENPIC NN + 3NFs at N²LO (E. Epelbaum, et al., PRC 99, 024314 (2019); arXiv:1807.02848)

LENPIC NN + 3NFs at N²LO (E. Epelbaum, et al., PRC 99, 024314 (2019); arXiv:1807.02848)

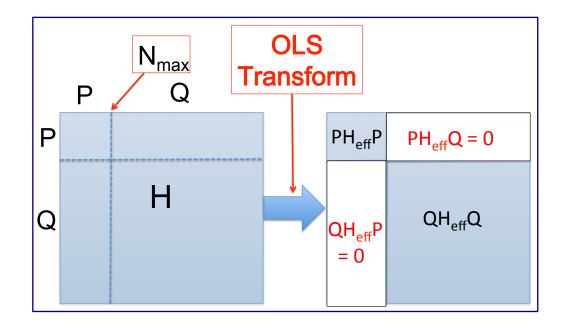


LENPIC NN + 3NFs at N²LO E. Epelbaum, et al., PRC 99, 024314 (2019); arXiv:1807.02848



OLS Transform:

Unitary transformation that block-diagonalizes the Hamiltonian – i.e. it integrates out Q-space degrees of freedom.



$$UHU^{\dagger} = U[T + V]U^{\dagger} = H_d$$
, the diagonalized H

$$H_{\text{eff}} \equiv U_{OLS} H U_{OLS}^{\dagger} = P H_{\text{eff}} P = P [T + V_{\text{eff}}] P$$

$$W^P \equiv PUP$$

$$\tilde{U}^P \equiv P \tilde{U}^P P \equiv \frac{W^P}{\sqrt{W^{P\dagger}W^P}}$$

$$H_{\text{eff}} = \tilde{U}^{P\dagger} H_d \tilde{U}^P = \tilde{U}^{P\dagger} U H U^{\dagger} \tilde{U}^P = P[T + V_{\text{eff}}] P$$

We conclude that:

$$U_{OLS} = \tilde{U}^{P\dagger}U$$

Similarly, we have effective operators for observables:

$$O_{ ext{eff}} \equiv \tilde{U}^{P\dagger} U O U^{\dagger} \tilde{U}^{P} = P[O_{ ext{eff}}] P$$

PRC98, 065502 (2018) arXiv:1809.00276 for applications

See: J.P. Vary, et al.,



Consider two nucleons as a model problem with V = LENPIC chiral NN solved in the harmonic oscillator basis with $\hbar\Omega$ = 5, 10 and 20 MeV. Also, consider the role of an added harmonic oscillator quasipotential

Hamiltonian #1
$$H=T+V$$
 Hamiltonian #2 $H=T+U_{\rm osc}(\hbar\Omega_{\rm basis})+V$

Other observables:

Root mean square radius	R
Magnetic dipole operator	M1
Electric dipole operator	E1
Electric quadrupole moment	Q
Electric quadrupole transition	E2
Gamow-Teller	GT
Neutrinoless double-beta decay	$M(0v2\beta)$

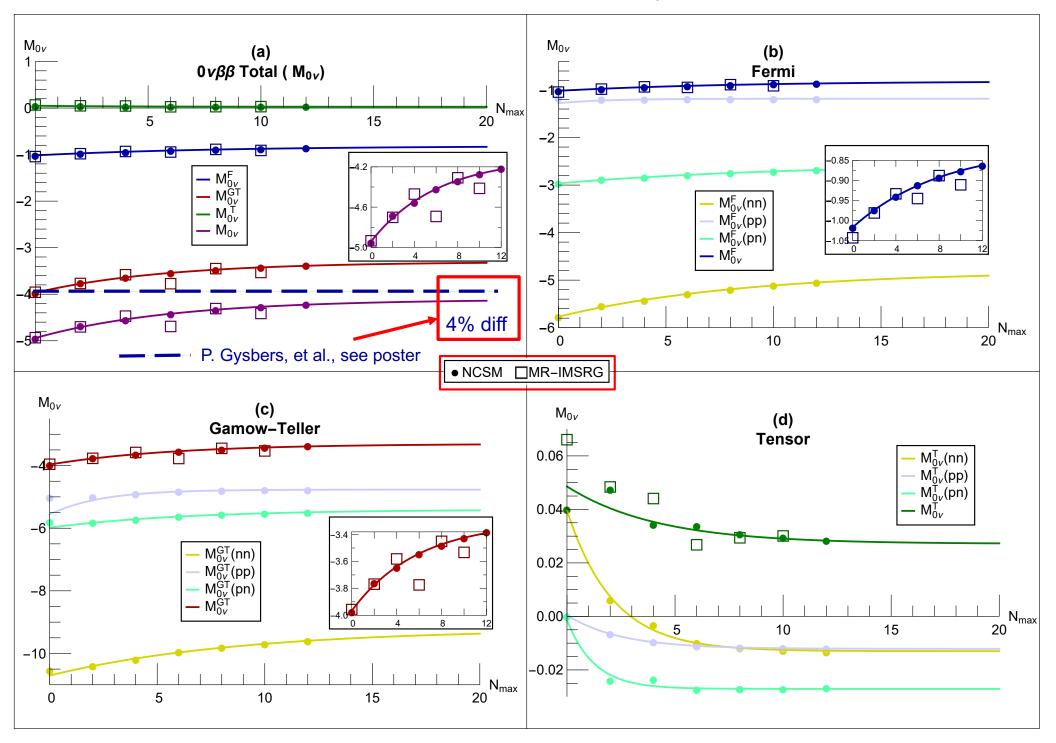
Dimension of the "full space" is 400 for all results depicted here

We initially considered a 2-body contribution within EFT to 0vββ-decay at N²LO G. Prézeau, M. Ramsey-Musolf and P. Vogel, Phys. Rev. D 68, 034016 (2003)

This operator is used in: J.P. Vary, et al., PRC98, 065502 (2018); Jon Engel's operator used in: ISU-UNC-MSU Collaboration benchmarking NCSM and MR-IMSRG (paper in preparation)

lowa State work-in-progress – take $0\nu\beta\beta$ -decay operators, term-by-term, available from V. Cirigliano, W. Dekens, J. de Vries, M.L. Graesser and E. Mereghetti, arXiv:1806.02780; calculate them in the harmonic oscillator basis and use LENPIC LECs for NCSM apps with LENPIC interactions.

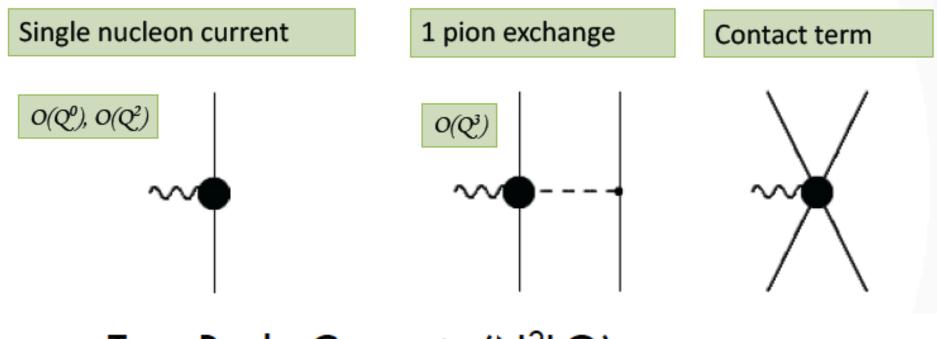
ISU – UNC – MSU collaboration to benchmark 0vββ-decay matrix elements for ⁶He -> ⁶Be



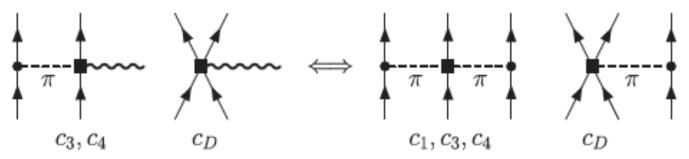
Coupling to External Probes in Chiral EFT

LENPIC collaboration (in process) – adopts momentum space regulators

□ Nuclear Axial Current Operators e.g. Krebs, et al., Ann. Phys. 378, 317 (2017)



Two-Body Currents (N²LO)



Note: we are working to retain dependence on external momentum transfer

Charge radius

► The charge radius squared is defined as the second moment of the charge form factor,

$$\langle r^2 \rangle = -\frac{dG_C(k^2)}{dk^2} \bigg|_{k^2=0}. \tag{4}$$

- ► The charge form factor is obtained from the scalar component of the charge operator.
- At leading order (Q^{-3}) the charge operator consists of point-like nucleons,

$$\hat{\rho}_{LO} = |e| \sum_{i} \frac{1 + \tau_{i}^{z}}{2} \delta(\vec{p}_{i}' - \vec{p}_{i} - \vec{k}).$$
 (5)

- There is no contribution to the charge operator at next-to-leading order.
- At N2LO (Q^{-1}) , there are relativistic corrections arising from the finite size of the nucleons, [Phillips, 2003]

$$\hat{\rho}_{N2LO} = -\frac{|e|}{6} \langle r_{Es}^2 \rangle \sum_i \frac{1 + \tau_i^z}{2} \delta(\vec{p}_i' - \vec{p}_i - \vec{k}). \tag{6}$$

Charge radius

ightharpoonup The first two body correction appears at N3LO (Q^0),

[Kölling *et.al.*, 2011]

$$\hat{\rho}_{N3LO} = \frac{|e|g_A^2}{16F_\pi^2 m_N} \left(1 - 2\bar{\beta}_9 \right)$$

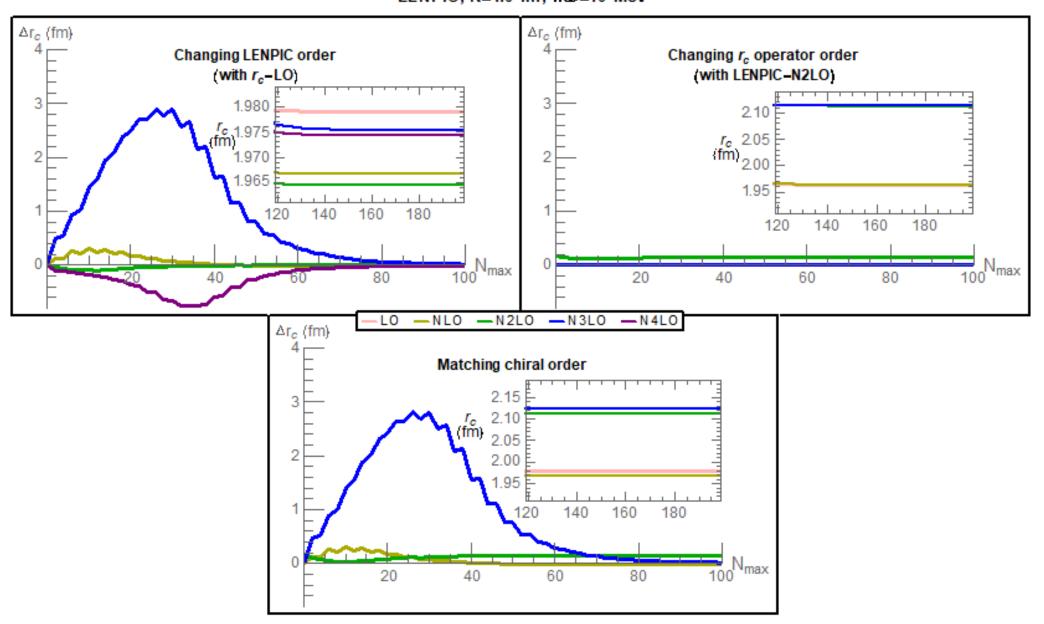
$$\sum_{i < j} \left\{ (\tau_i^z + \vec{\tau}_i \cdot \vec{\tau}_j) \frac{\vec{\sigma}_i \cdot \vec{q}_i \vec{\sigma}_j \cdot \vec{k}}{q_i^2 + m_\pi^2} + i \leftrightarrow j \right\}$$

$$\delta(\vec{p}_i' + \vec{p}_j' - \vec{p}_i - \vec{p}_j - \vec{k}).$$
(7)

- $ar{eta}_9$ is a parameter of the unitary transformation used to renormalize the one-pion exchange potential, and the charge operator. We have used $ar{eta}_9=0$.
- ► There are two more terms that contribute to the charge operator at N3LO, however they do not contribute to the charge radius.



Deuteron rms charge radius (r_c) $\Delta r_c^{\lambda} = r_c^{\lambda} - r_c^{\lambda-1}$ LENPIC, R=1.0 fm, $\hbar \omega$ =10 MeV



Gamow-Teller transition

- We consider the operators at zero momentum transfer.
- ► The leading order contribution (Q^{-3} in power counting) obtained from chiral EFT coincides with the impulse approximation operator,

$$\hat{O}_{GT,LO}^{\pm} = -g_A \sum_{i} \tau_i^{\pm} \hat{\sigma}_i \delta(\vec{p}_i' - \vec{p}_i). \tag{1}$$

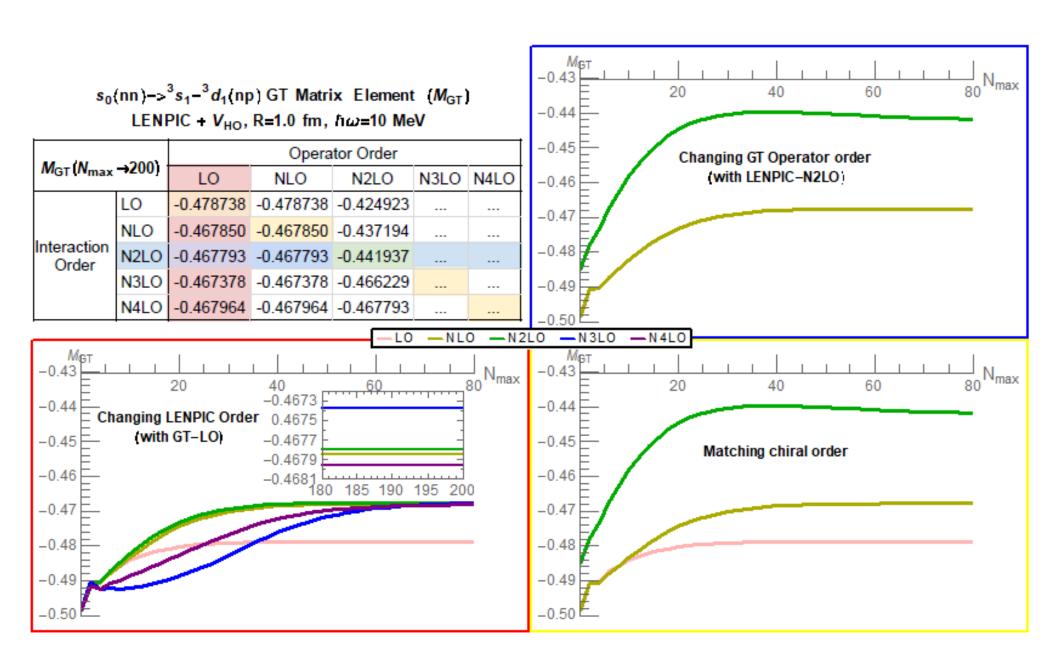
► The first two body correction from chiral EFT appears at N2LO (Q⁰ in power counting), [Krebs, et.al., 2017]

$$\hat{O}_{GT,N2LO}^{\pm} = -\frac{1}{2(2\pi)^3} D \sum_{i < j} \left(\tau_i^{\pm} \hat{\sigma}_i + i \leftrightarrow j \right) \delta(\vec{p}_i' + \vec{p}_j' - \vec{p}_i - \vec{p}_j). \tag{2}$$

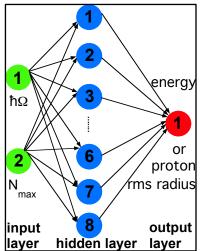
► The low energy constant *D* comes from the one pion exchange loop diagram, and is usually expressed in terms of a more well-known low energy constant, *c*_D,

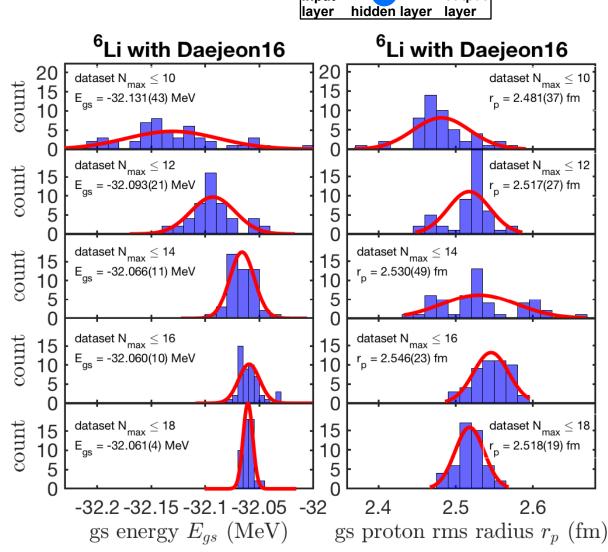
$$D = \frac{c_D}{F_\pi^2 \Lambda_\chi}. (3)$$

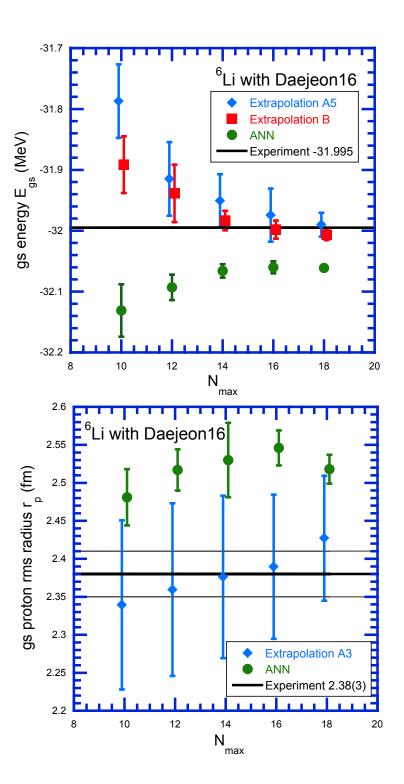
We have used $c_D = -1$ [Navratil *et.al.*, 2007 and the chiral symmetry breaking scale $\Lambda_{\infty} = 700$ MeV.



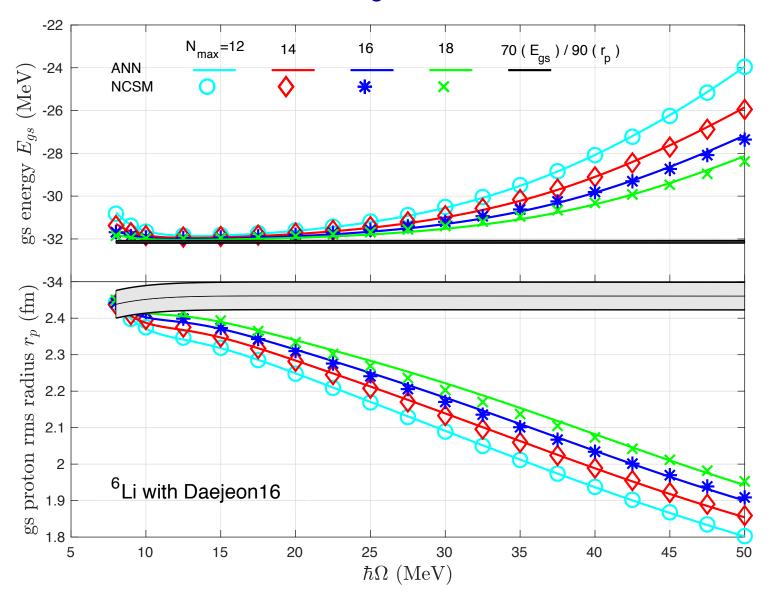
Deep Learning: Extrapolation Tool for Ab Initio Nuclear Theory, G.A. Negoita, et al., arXiv:1810.04009







ANN results when training data limited to Nmax ≤ 10



G.A. Negoita, et al., "Deep Learning: Extrapolation Tool for Computational Nuclear Physics," submitted to PRC; arXiv: 1811.01782

Progress:

LENPIC NN+NNN (at N2LO) paper: PRC accepted; arXiv:1807.02848

Completed studies of model 2-body systems: PRC98, 065502 (2018); arXiv: 1809:00276

Implement electroweak operators in finite nuclei:

Benchmark A=6 calculations of $0v2\beta$ -decay with UNC & MSU groups (paper in preparation)

Postprocessor code for scalar and non-scalar observables (in testing stage) lowa State – Notre Dame collaboration

Develop extrapolations and uncertainties with Artificial Neural Networks: A. Negoita, et al., submitted to PRC; arXiv:1810.04009

Outlook:

Expand treatment to full range of EW operators within Chiral EFT at NLO, N2LO & N3LO (studies underway)

Extend effective EW operator approach to medium weight nuclei with "Double OLS" approach (sd shell investigations underway: N. Smirnova, et al)

Iowa State University Members of NUCLEI and Topical Collaboration Teams

Faculty

J.P. Vary and P. Maris

Grad Students

Robert Basili
Weijie Du
Mengyao Huang
Matthew Lockner
Alina Negoita
Soham Pal
Shiplu Sarker

New faculty position at Iowa State in Nuclear Theory Supported, in part, by the Fundamental Interactions
Topical Collaboration
Interviews in process

Breaking News

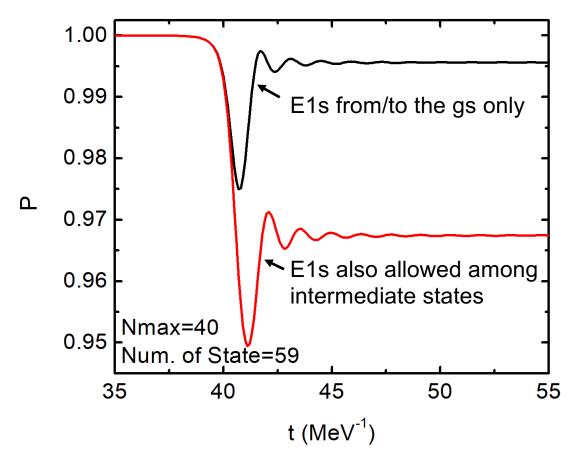
Time-Dependent Basis Function approach to Coulomb Excitation

Deuteron (JISP16) on 208 Pb target E_d (lab) = 12 MeV, Lab scattering angle of n-p CM = 70° Peng Yin, et al., in preparation

P = probability the deuteron remains in the elastic channel as function of t.

Non-perturbative treatment of electric dipole transitions to continuum states.

1-P = breakup probability



W. Du, et al., PRC 97, 064620 (2018); arXiv 1804.01156